<u>19th International Congress on</u> Insurance: Mathematics and Economics (IME) 2015 <u>Abstract Submission</u>

Title: Fourier-cosine method for Gerber-Shiu functions

Authors:

- 1. Mr. K. W. CHAU
 - (a) Affiliation: Department of Mathematics, The University of Hong Kong, Pokfulam, Hong Kong
 - (b) Postal address: Department of Mathematics, Run Run Shaw Building, The University of Hong Kong, Pokfulam Road, Hong Kong
 - (c) Email address: kiwichau@connect.hku.hk
 - (d) Telephone number: +852 63580920
- 2. Prof. Phillip YAM
 - (a) Affiliation: Department of Statistics, The Chinese University of Hong Kong, Shatin, NT, Hong Kong
 - (b) Postal address: Room G19, Lady Shaw Building, The Chinese University of Hong Kong, Shatin, NT, Hong Kong
 - (c) Email address: scpyam@sta.cuhk.edu.hk
 - (d) Telephone number: +852 39437941
- 3. Prof. H. YANG
 - (a) Affiliation: Department of Statistics and Actuarial Science, The University of Hong Kong, Pokfulam, Hong Kong
 - (b) Postal address: Room 232, Department of Statistics and Actuarial Science, Run Run Shaw Building, The University of Hong Kong, Pokfulam Road, Hong Kong
 - (c) Email address: hlyang@hku.hk
 - (d) Telephone number: +852 39178322

Corresponding IME session speaker: Phillip YAM

Abstract: In this talk, we introduce a systematic study on effectively approximating the Gerber-Shiu functions, which is a hardly touched topic in the current literature, by incorporating the recently popular Fourier-cosine method. Fourier-cosine method has been a prevailing numerical method in option pricing theory since the work of Fang and Oosterlee (2009). Our approximant of Gerber-Shiu functions under Lévy subordinator model has O(n) computational complexity in comparison with that of $O(n \log n)$ via the fast Fourier transform algorithm. Also, for Gerber-Shiu functions within our proposed refined Sobolev space, we introduce an explicit error bound, which seems to be absent from the literature. In contrast with our previous work (Chau et al., 2015), this error bound is more conservative without making heavy assumptions on the Fourier transform of the Gerber-Shiu function. Further numerical studies will be included.

Keywords: Gerber-Shiu functions; Lévy subordinator; Fourier-cosine method; Sobolev embedding theorem; Harmonic analysis.