

# Modelling prokaryote gene content

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# Acknowledgements

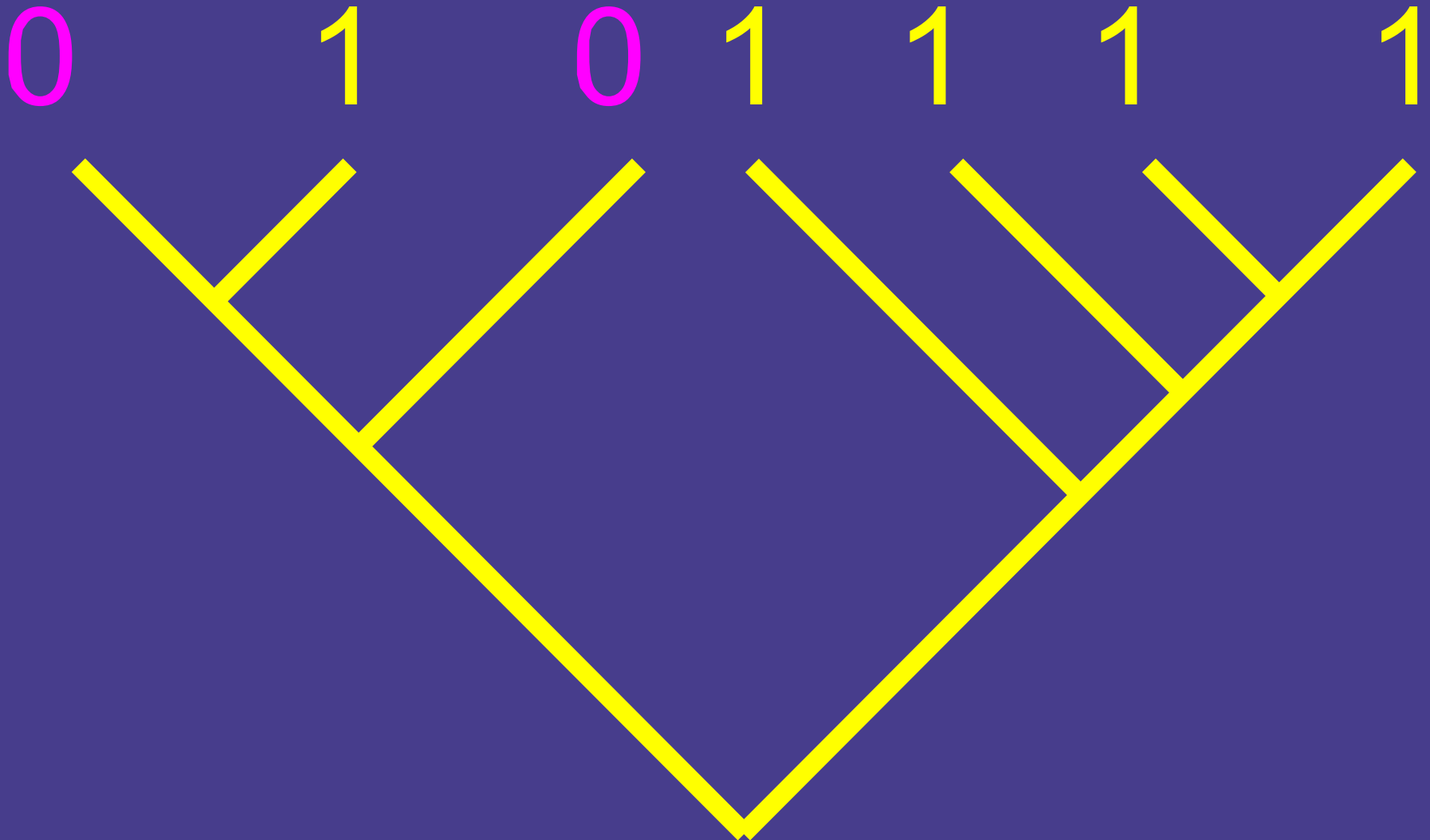
- Andrew Roger
- Ed Susko
- Dalhousie Statistical Evolutionary Bioinformatics group
- Genome Atlantic

# Outline

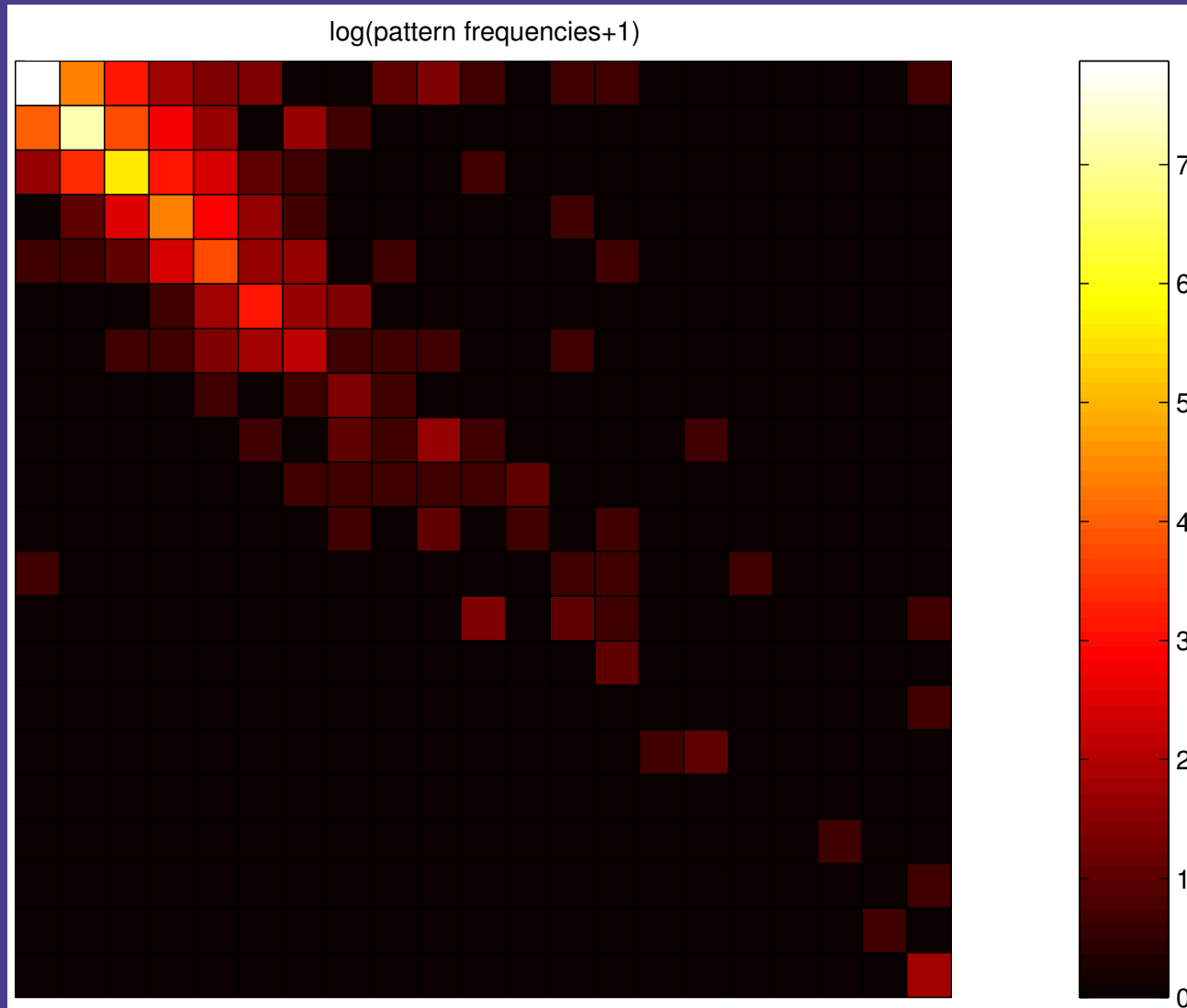
- Gene distributions: lateral transfer or multiple loss?
- Birth-death models vs. models with multi-gene events
- Lateral transfer rates
- ML distance phylogenies
- Residence times of genes

<http://www.mathstat.dal.ca/~matts/>

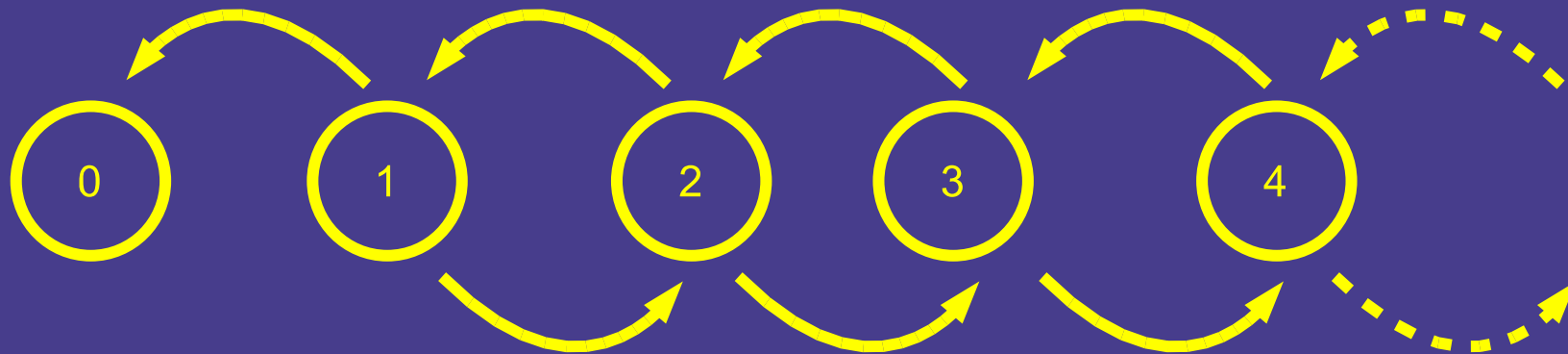
# Lateral transfer or gene loss?



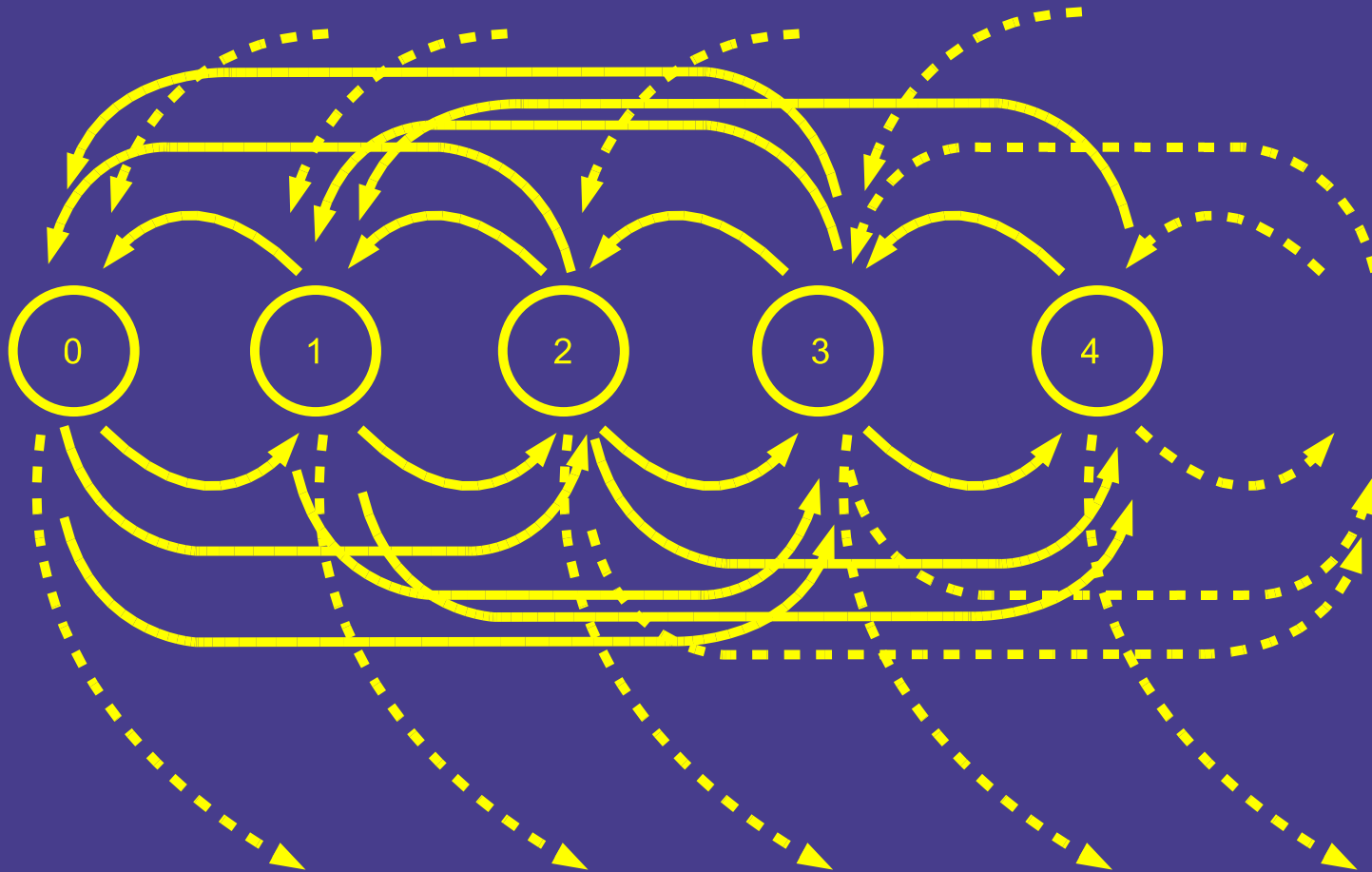
# Gene family size data



# Birth-death model



# Models with multi-gene events



# Assumptions

- Family independence
- Finite maximum number of genes in family
- Frequent rearrangements
- Lateral transfers come from outside the set of sampled organisms



# Rate categories

- Deletions of single genes
- Gains of single genes
- Deletions of  $> 1$  gene
- Gains of  $> 1$  gene where the gain could be duplication
- Gains of more genes than could be duplicated
- Loss of entire gene family
- Transition from 0 to 1 members of family

# Results

Log likelihoods:

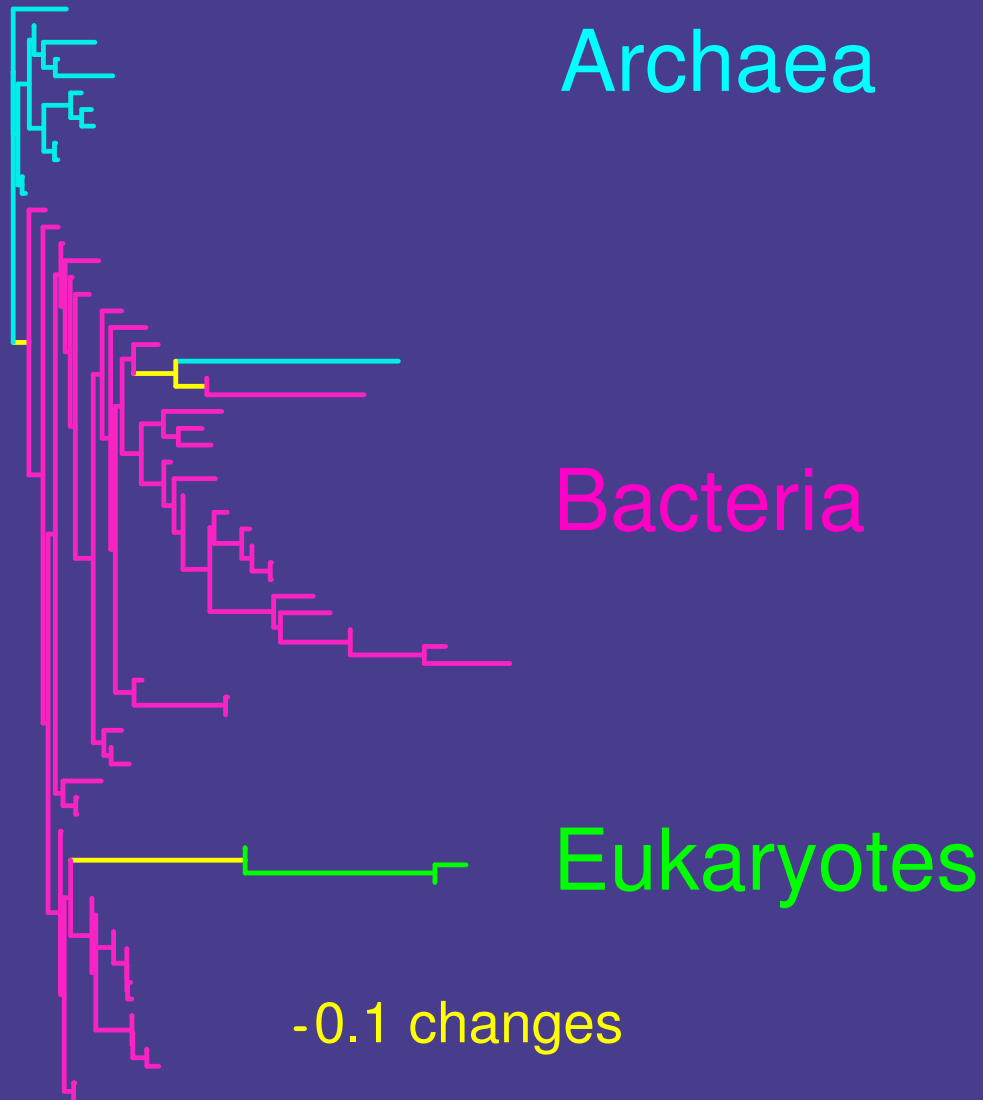
Species	blocks	birth-death
<i>E. coli</i>	$-7.55 \times 10^3$	$-7.89 \times 10^3$
<i>A. fulgidus</i> & <i>B. subtilis</i>	$-9.13 \times 10^3$	$-9.17 \times 10^3$

- Strongly prefer blocks model for both pairs
- Evidence for deletions and duplications of multiple genes

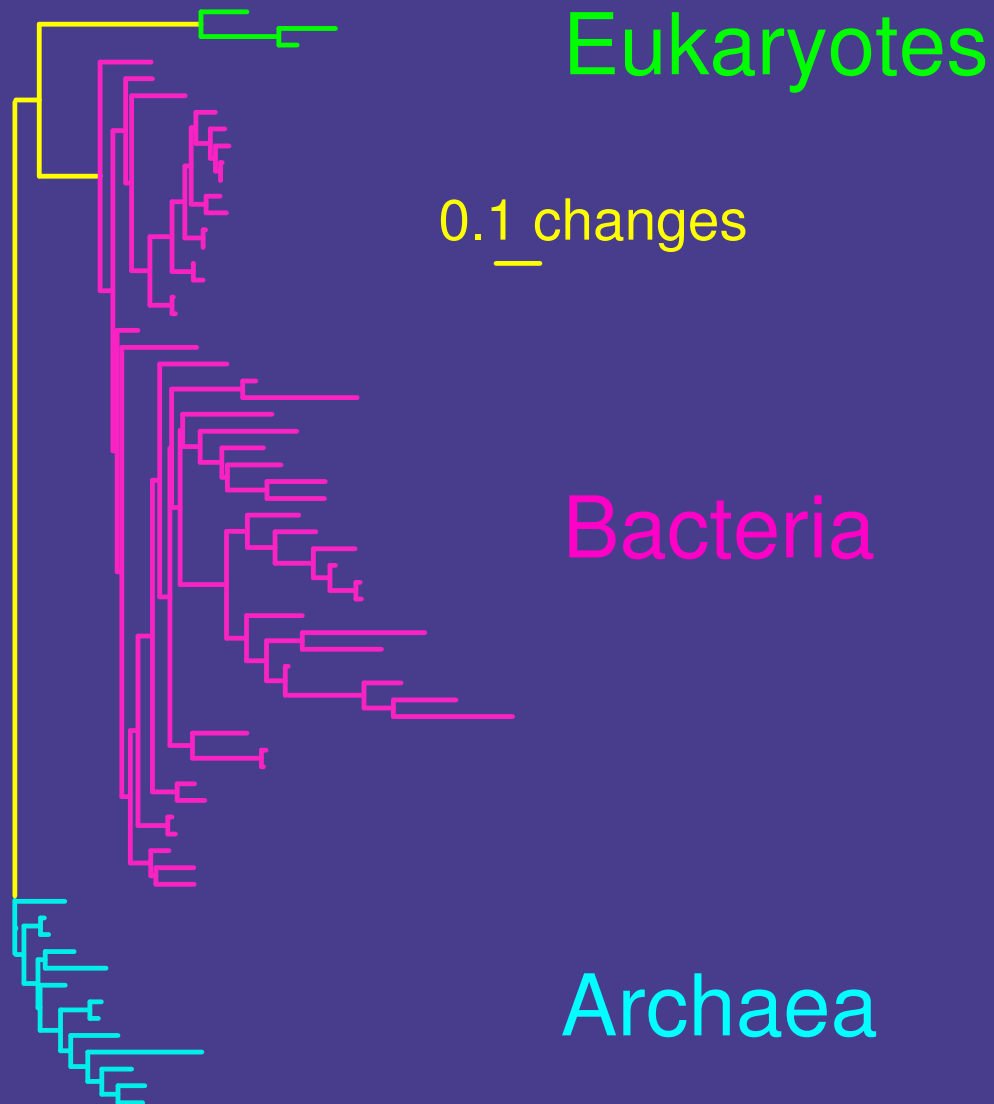
# Lateral transfer rates?

Species	multiple genes	0 → 1
<i>E. coli</i>	$5.21 \times 10^{-4}$	0.27
<i>A. fulgidus</i> & <i>B. subtilis</i>	$6.79 \times 10^{-8}$	0.40

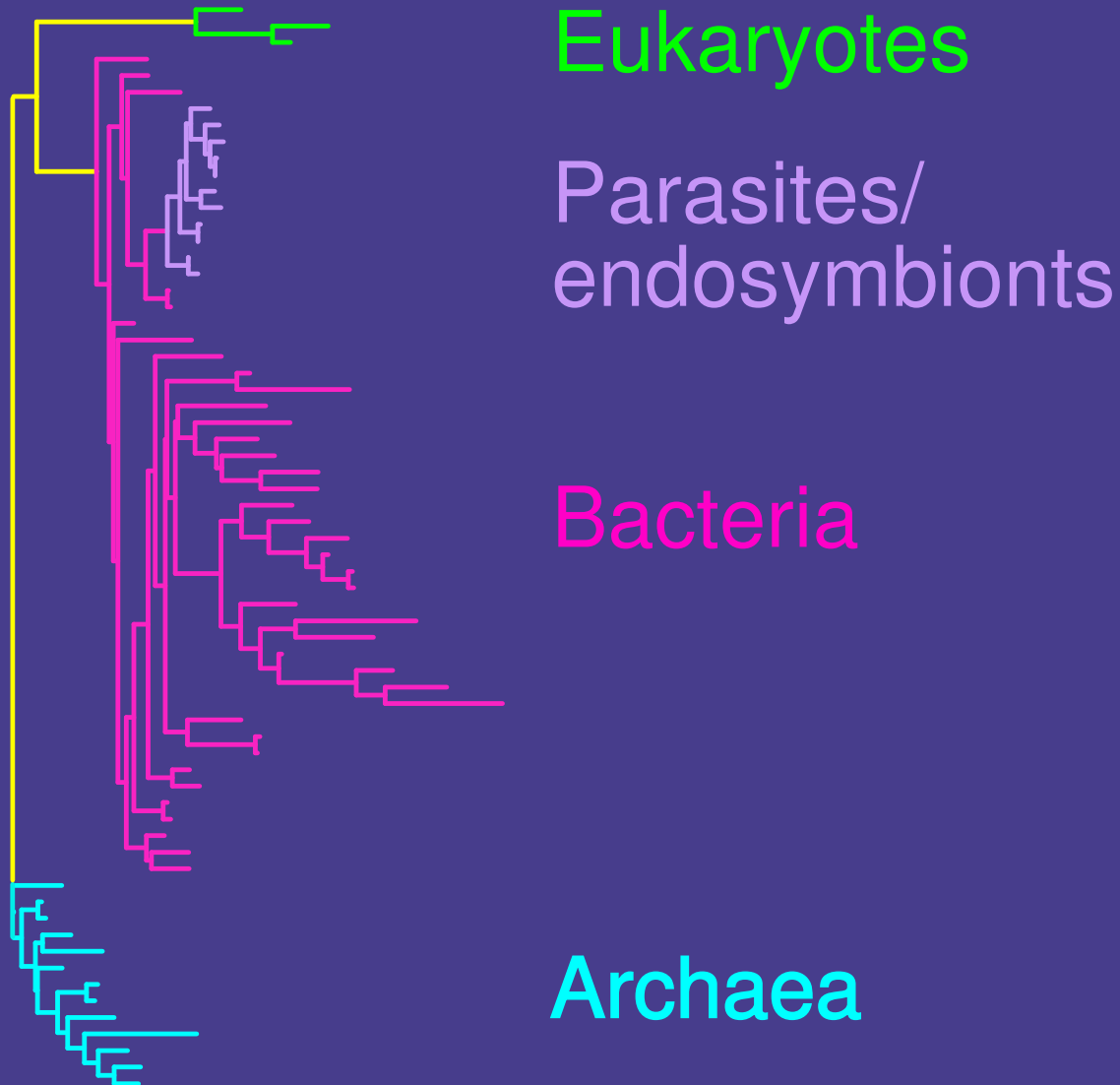
# Birth-death phylogeny



# Blocks phylogeny



# Blocks phylogeny



# Residence times

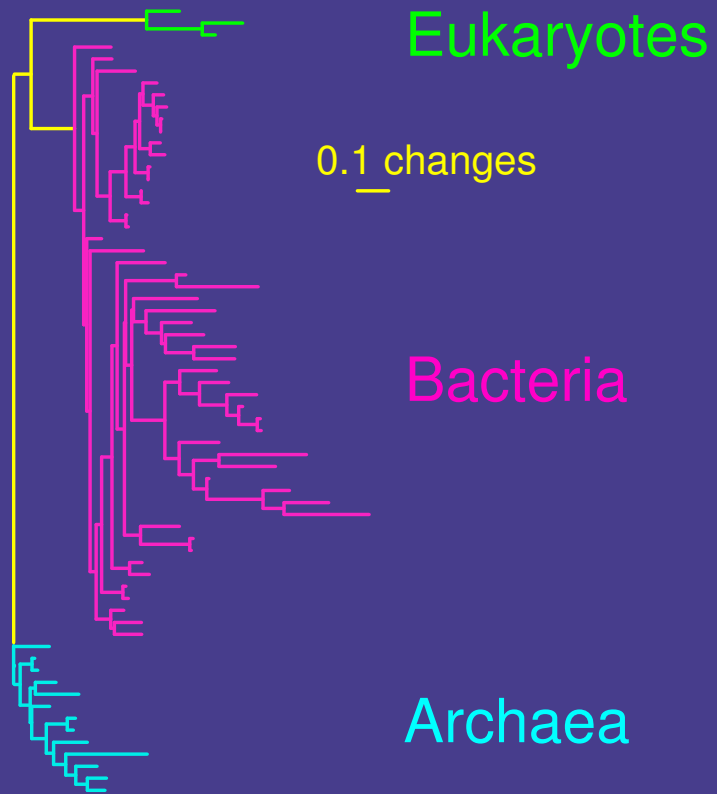
- Expected time from origin of a gene (innovation, duplication or transfer) to loss from the genome
- = sum over all states  $i$  [(probability we enter state  $i$  as a new gene is created)  $\times$  (expected time to lose a gene created in state  $i$ )]
- *E. coli*: mean 0.60, median 0.33 events
- *A. fulgidus/B. subtilis*: mean 0.48, median 0.34 events
- Between ancestors of bacteria and archaea: 0.19 events

# Summary

- Models that allow multi-gene events work better than birth-death models
- No evidence for frequent transfers of multiple genes from the same family
- May be a high rate of lateral transfers of single genes
- If we want to use single genes, we should focus on the ones with long residence times

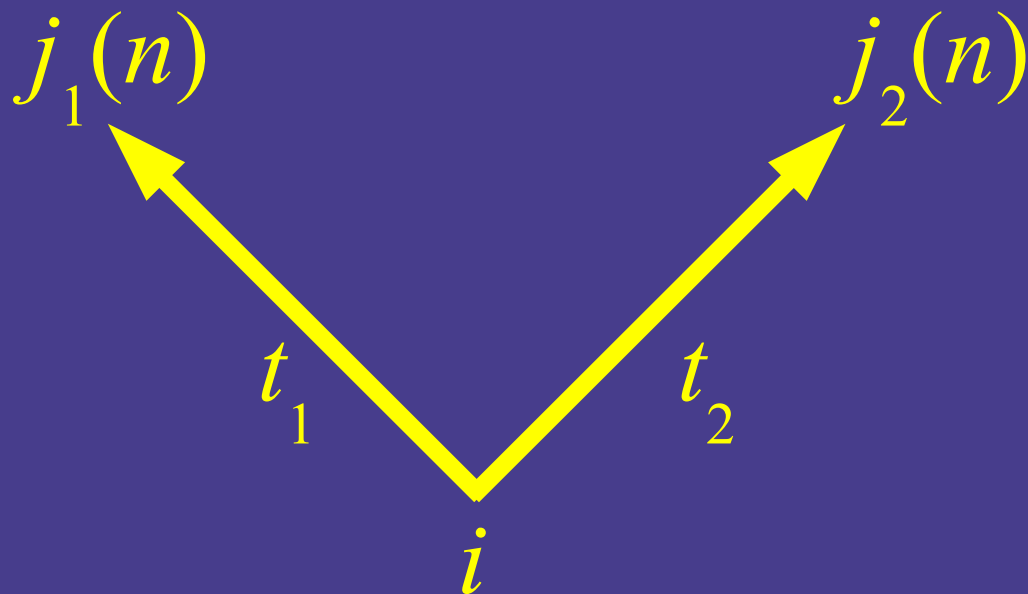


# The End



<http://www.mathstat.dal.ca/~matts/>

# Likelihood calculation



$$L = \prod_{n=1}^N \sum_{i=0}^k \pi_i P(i, j_1(n) | t_1) P(i, j_2(n) | t_2)$$

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- Sum over possible root states  $i$
- Product over all gene families  $n$

# Residence times

$$E(r) = \sum_{i=0}^k \beta_i r_i$$

where  $\beta_i$  is the probability that we enter state  $i$  as a gene appears in the genome, and  $r_i$  is the expected time until a gene is deleted, given that we were in state  $i$  when it appeared in the genome.



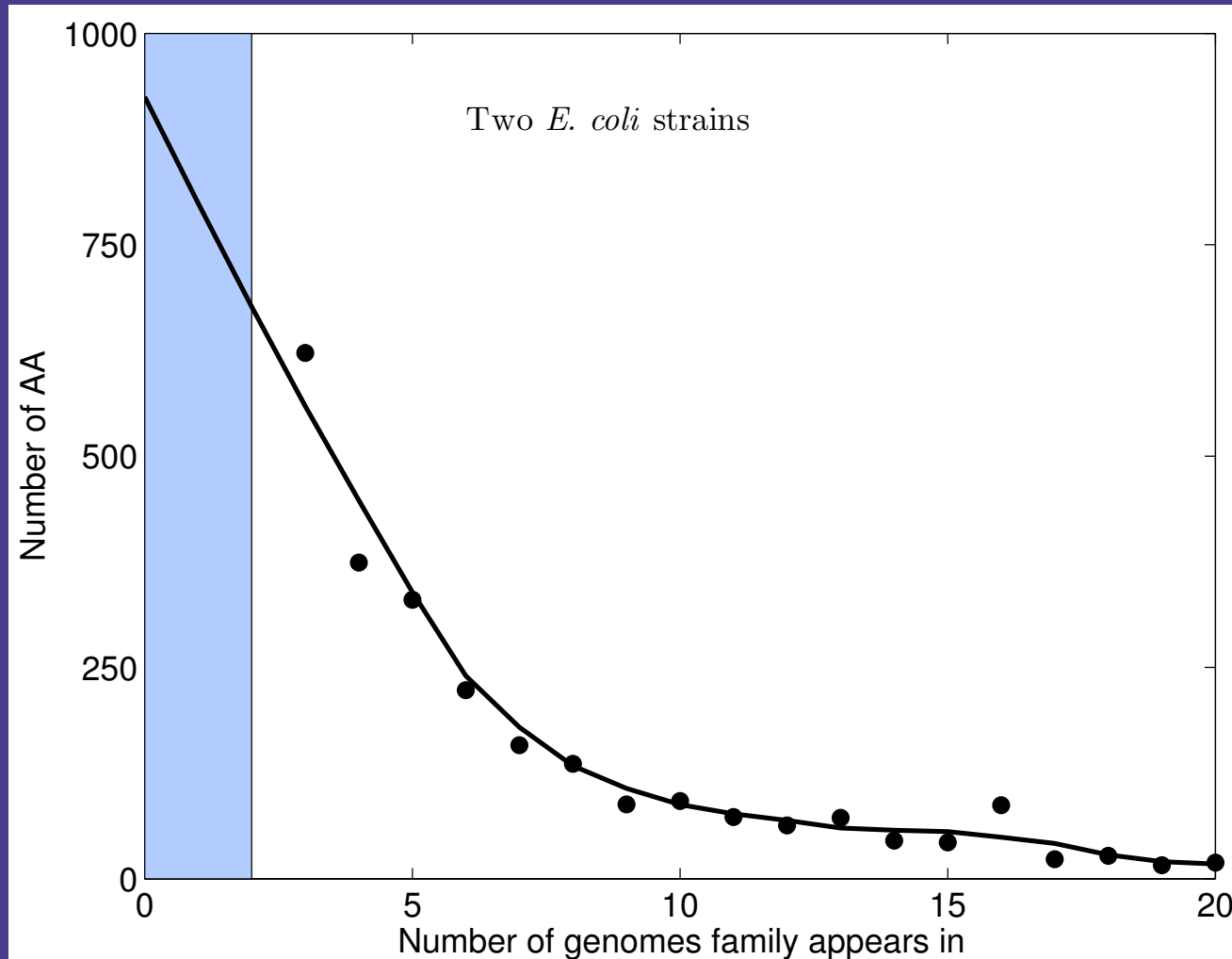
# Residence times

At steady state,

$$\beta_i = \sum_{j < i} q_{ji} \pi_j (i - j) / \sum_i \sum_{j < i} q_{ji} \pi_j (i - j)$$

The numerator is the sum of steady-state rates of flow into state  $i$  that add new genes, weighted by the number of genes  $i - j$  each flow adds. The denominator normalizes the  $\beta_i$  to probabilities.

# Unobservable data by extrapolation



# Residence time distribution

