## Practice Class Test MATH102 2008

1. Write down the Taylor series at 0 of  $f(x) = \sin 2x$ .

[3 marks] 2. Write down the quadratic Taylor poynmial  $P_2(x) = P_2(x, 4)$  near x = 4 for  $f(x) = x^{1/2}$ , and work out  $P_2(3)$ . Write down an expression for the remainder term  $R_2(3)$ . Now find an upper bound on  $|R_2(3)|$  and hence show that

$$|\sqrt{3} - P_2(3)| \le \frac{1}{16 \times 3^{5/2}} < 0.005.$$

Confirm this by using your calculator to compute  $\sqrt{3}$ .

[9 marks]

3. Solve

$$x\frac{dy}{dx} + y^2 = 0, \quad y(1) = 2.$$

[5 marks]

4. Solve

$$x\frac{dy}{dx} - y = x^2, \quad y(2) = 1$$

[7 marks]

5. Find the general solution to

$$\frac{d^2y}{dx^2} - 4\frac{dy}{dx} + 5y = 0.$$

[4 marks]

6. Find the general solution to

$$\frac{d^2y}{dx^2} + 2\frac{dy}{dx} + y = e^{2x}.$$

[6 marks]

7. Show that

$$\frac{x^2 - xy}{x^2 + y^2}$$

does not exist, by calculating limits along two different directions at (0, 0). [4 marks]