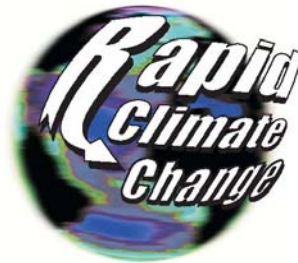


# Climate forcing from carbon emissions



Philip Goodwin<sup>1</sup>

Thanks to:

Ric Williams<sup>1</sup>,

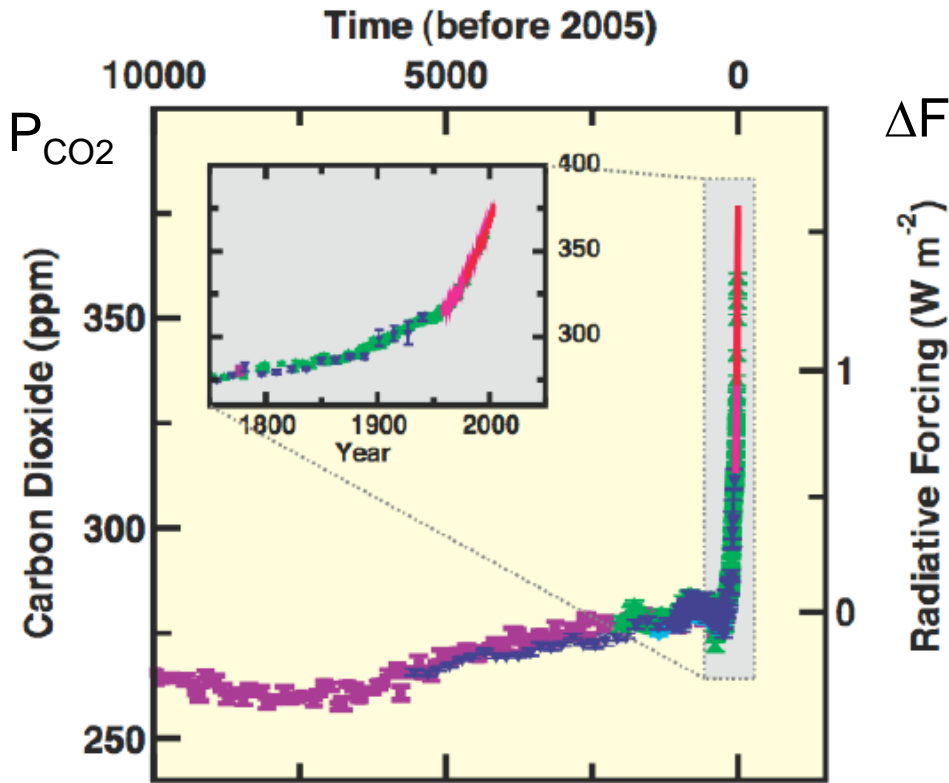
Mick Follows<sup>2</sup>, Andy Ridgwell<sup>3</sup>, Stephanie Dutkiewicz<sup>2</sup>

<sup>1</sup>University of Liverpool

<sup>2</sup>Massachusetts Institute of Technology, USA

<sup>3</sup>University of Bristol

# Rising atmospheric carbon dioxide ( $P_{CO_2}$ ): Anthropogenic projection



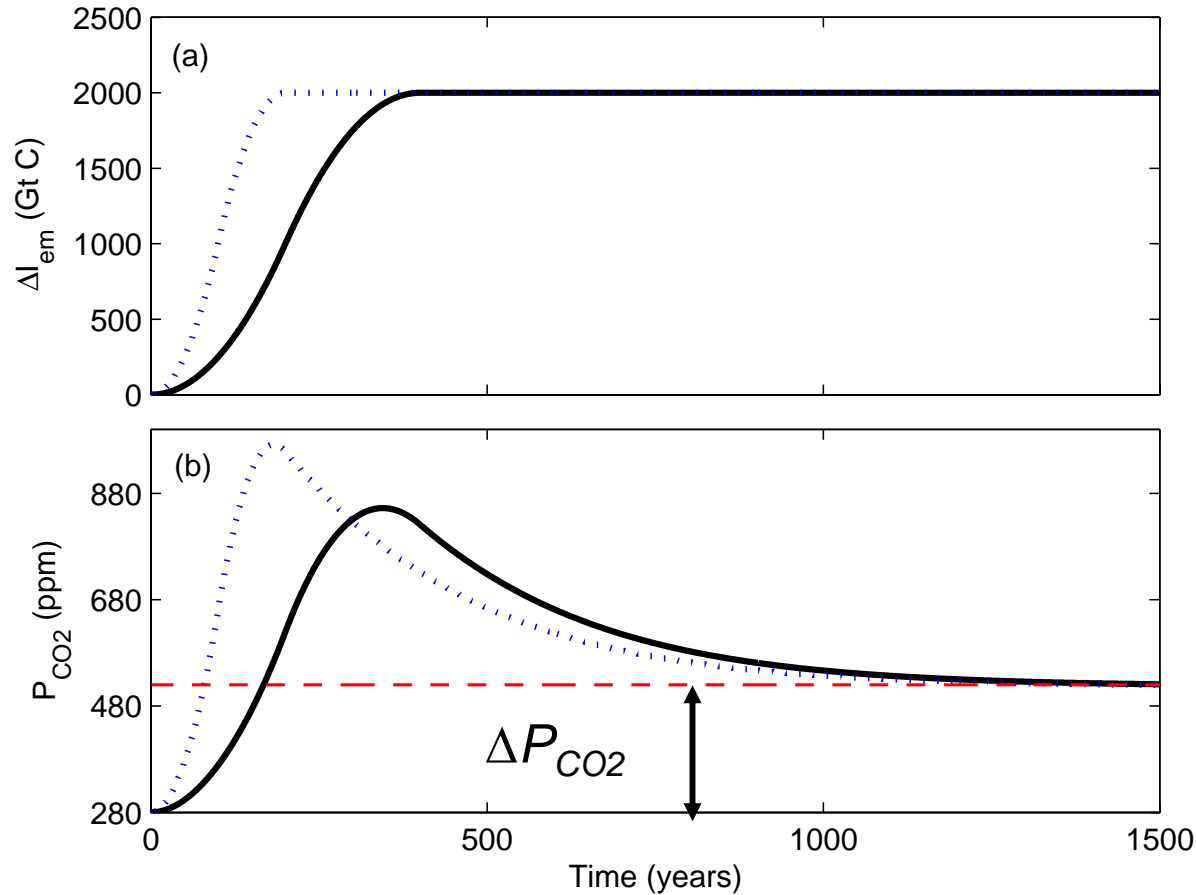
[IPCC 2007]

Aims:

- A) Relate emissions to 'steady state'  $P_{CO_2}$
- B) Consider radiative forcing
- C) Consider feedbacks
- Ignore carbonate and silicate rock weathering

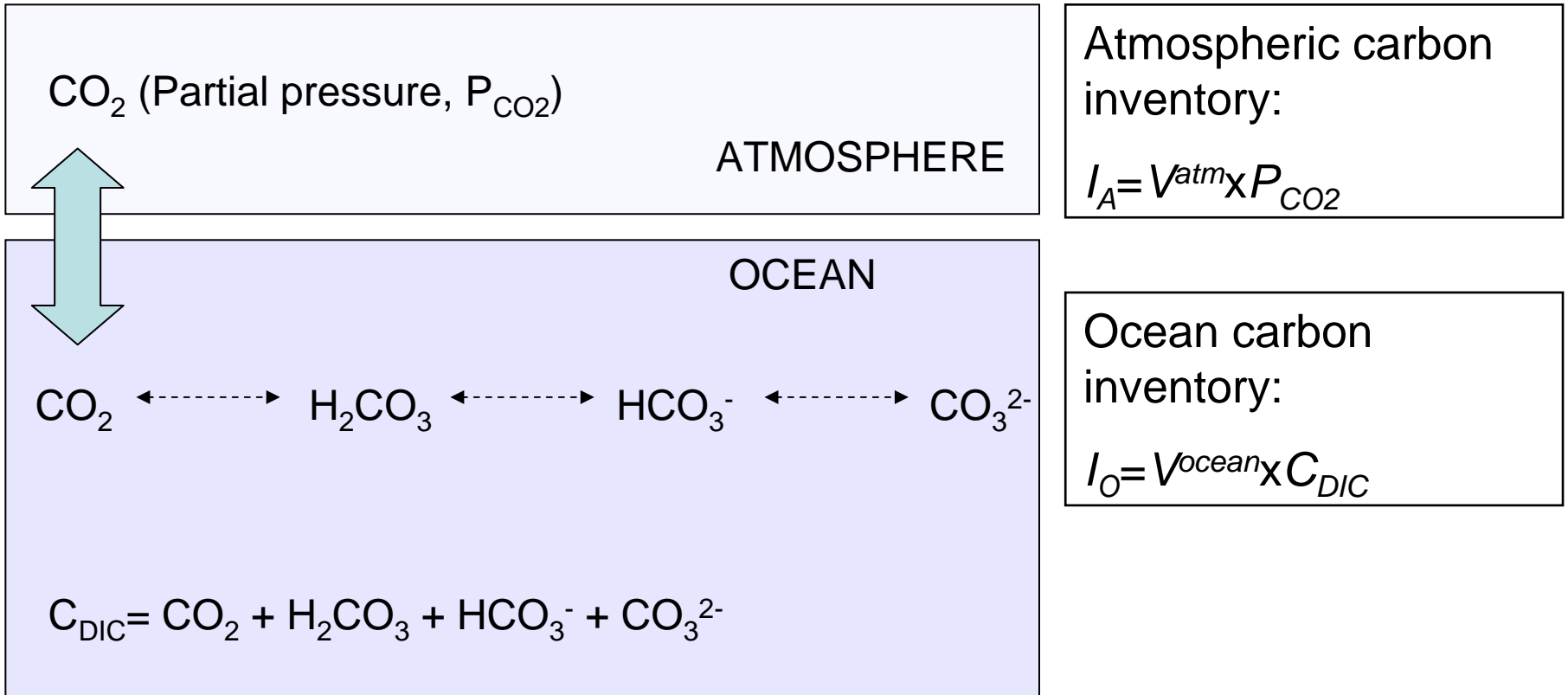
The rise in partial pressure of atmospheric  $CO_2$  ( $P_{CO_2}$ ) causes a radiative forcing ( $\Delta F$ ) which alters climate

For the same  $\Delta I_{em}$ , eventually same steady state  $P_{CO_2}$



Air-sea model response to a  $\Delta I_{em} = 2000\text{GtC}$  EMISSION: Same steady state

## Carbon in the atmosphere and ocean



- A steady state is reached when:

$$P_{CO_2} \propto [CO_2]_{ocean}$$

## Emissions without ocean chemistry

Steady state when:

$$P_{CO_2} \propto [CO_2]$$

Therefore:  $P_{CO_2} \propto I_A \propto I_O$

Thus  $P_{CO_2}$  proportional to total air-sea carbon:

$$P_{CO_2} \propto (I_O + I_A)$$

And:

$$\delta P_{CO_2} \propto \delta(I_O + I_A)$$

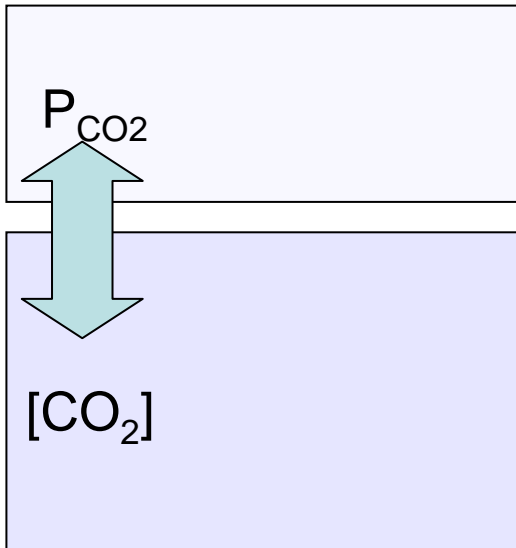
We can make a ratio:

$$\frac{\delta P_{CO_2}}{P_{CO_2}} = \frac{\delta(I_A + I_O)}{I_A + I_O}$$

Change in air-sea carbon is emission,

$$\delta I_{em} = \delta(I_A + I_O):$$

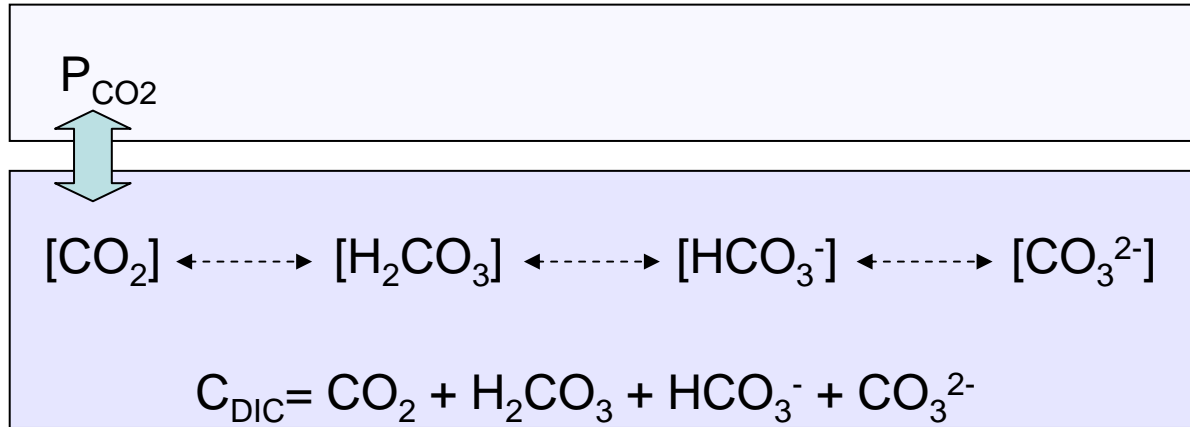
Therefore we can write:  $\delta \ln |P_{CO_2}| = \frac{\delta I_{em}}{I_A + I_O}$



Special case;

$$I_O = V^{ocean} \chi [CO_2]$$

## Emissions with ocean chemistry



At steady state:

$$P_{CO_2} \propto [CO_2]$$

But:

$$P_{CO_2} \not\propto I_A + I_O$$

We must define a **new** inventory,  $I_B$  [Goodwin et al, 2007], that accounts for the dissociation of  $CO_2$  in seawater

NO OCEAN CHEMISTRY

:

OCEAN CHEMISTRY

$$I_A + I_O$$



$$I_B = I_A + \frac{I_O}{B}$$

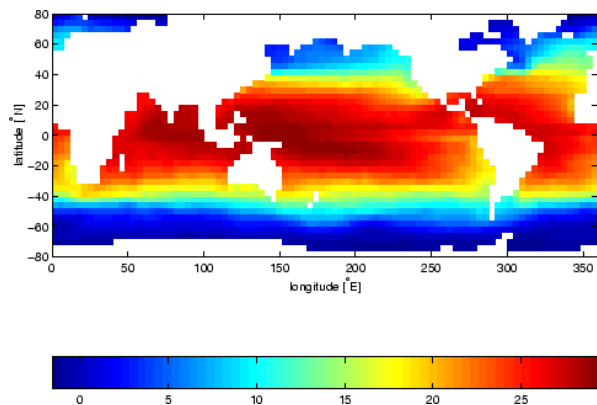
WHERE:  $B = \frac{\delta P_{CO_2}}{\delta C_{DIC}} \frac{C_{DIC}}{P_{CO_2}}$

$$\delta \ln |P_{CO_2}| = \frac{\delta I_{em}}{I_A + I_O}$$



$$\delta \ln |P_{CO_2}| = \frac{\delta I_{em}}{I_B}$$

# GCM experiment: how $P_{CO_2}$ links to carbon emission

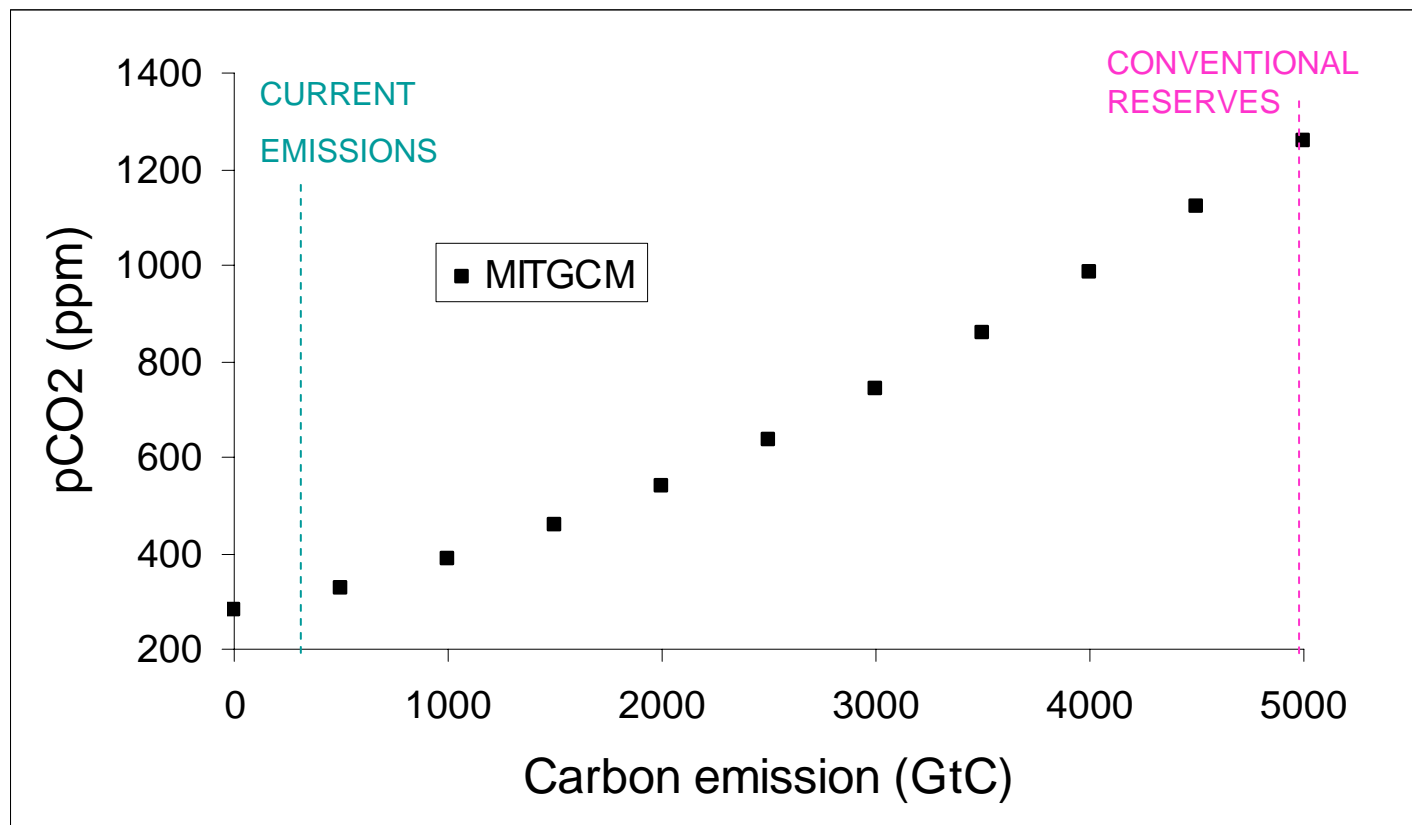


SURFACE  
TEMPERATURE  
(°C)

MIT GCM

- Realistic circulation
- Realistic carbon cycling
- Monthly mean forcing

- Add carbon to atmosphere over ~500 years
- Integrate for ~3000 years for steady state
- Measure final  $P_{CO_2}$

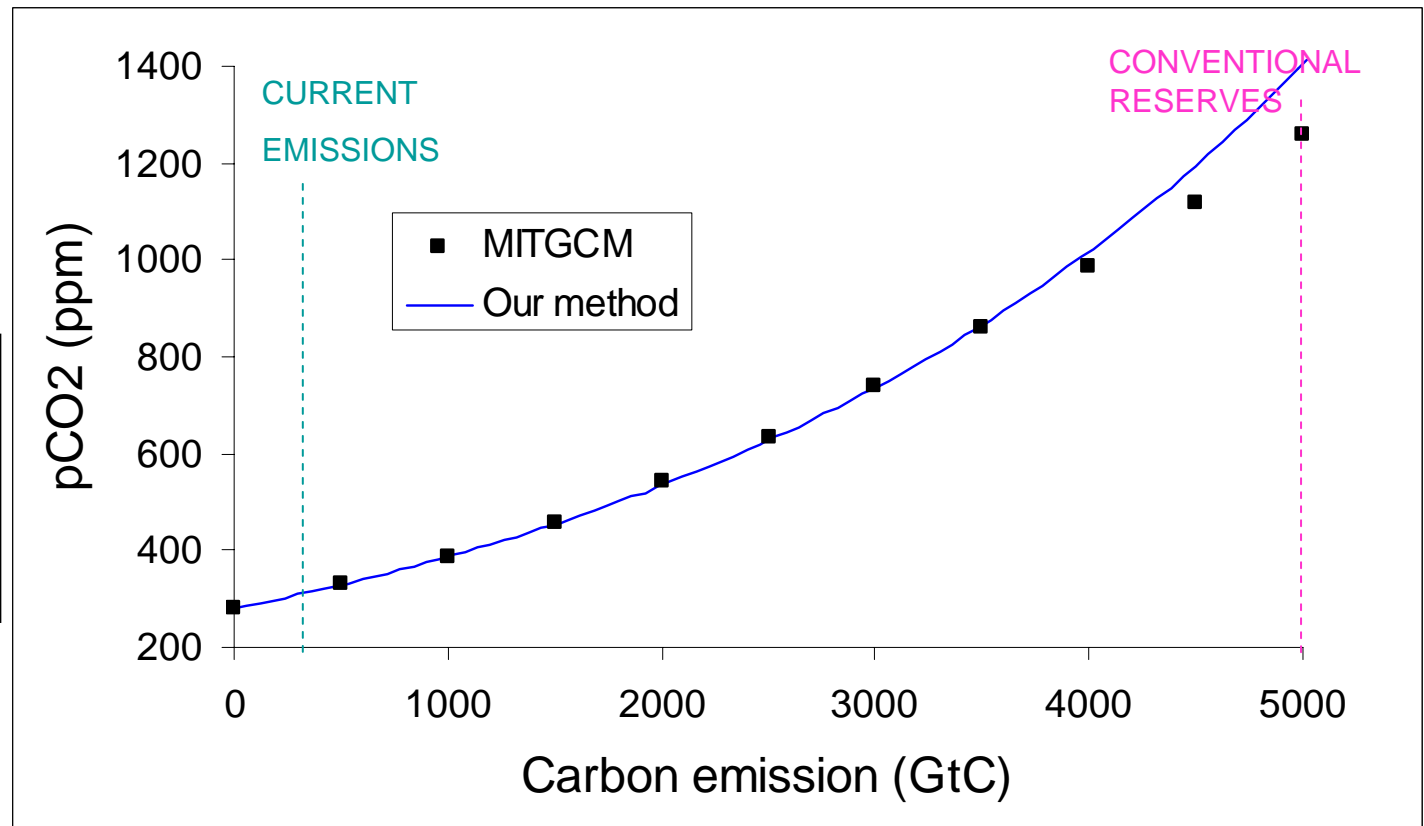
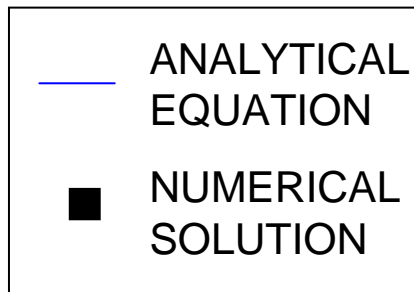


## Testing the independent analytical equation

- Evaluate  $I_B$  at pre-industrial steady state for MITGCM
- integrate by assuming  $I_B$  remains constant [Goodwin et al, 2007]:

$$\Delta \ln |P_{CO_2}| = \frac{\Delta I_{em}}{I_B} \quad \longrightarrow \quad P_f = P_i \exp\left(\frac{\Delta I_{em}}{I_B}\right)$$

Compare to  
model results:





## How can CO<sub>2</sub> affect climate?

Add CO<sub>2</sub> → Radiation imbalance,  $\Delta F$  → Temperature increases,  $\Delta T$

How do  $P_{CO_2}$  levels affect  $\Delta F$  (and so  $\Delta T$ )?

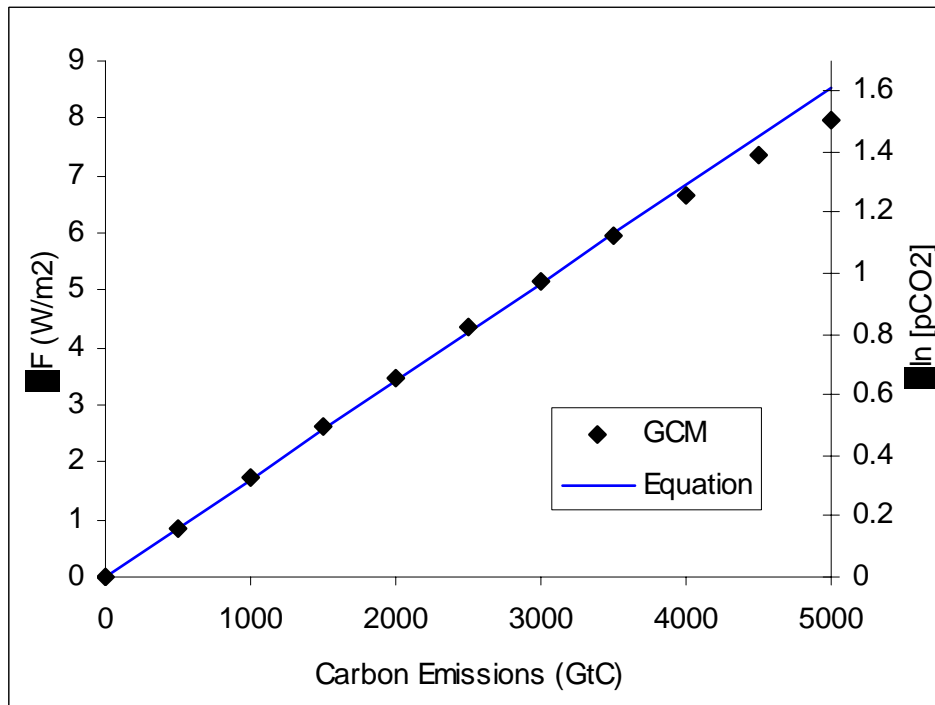
$$\Delta F = \alpha \Delta \ln |P_{CO_2}|$$

[Myhre et al, 1998]

Why logarithmic?

- CO<sub>2</sub> only absorbs at certain wavelengths
- Amount of those wavelengths in atmosphere reduces with increasing  $P_{CO_2}$
- An increase in  $P_{CO_2}$  absorbs set fraction of *what is left* in the atmosphere

**Therefore, write equations in log form.**

How about Radiative forcing?

From:

$$\Delta F = \alpha \Delta \ln |P_{CO_2}|$$

$$\frac{\Delta I_{em}}{I_B} = \Delta \ln |P_{CO_2}|$$

We get:

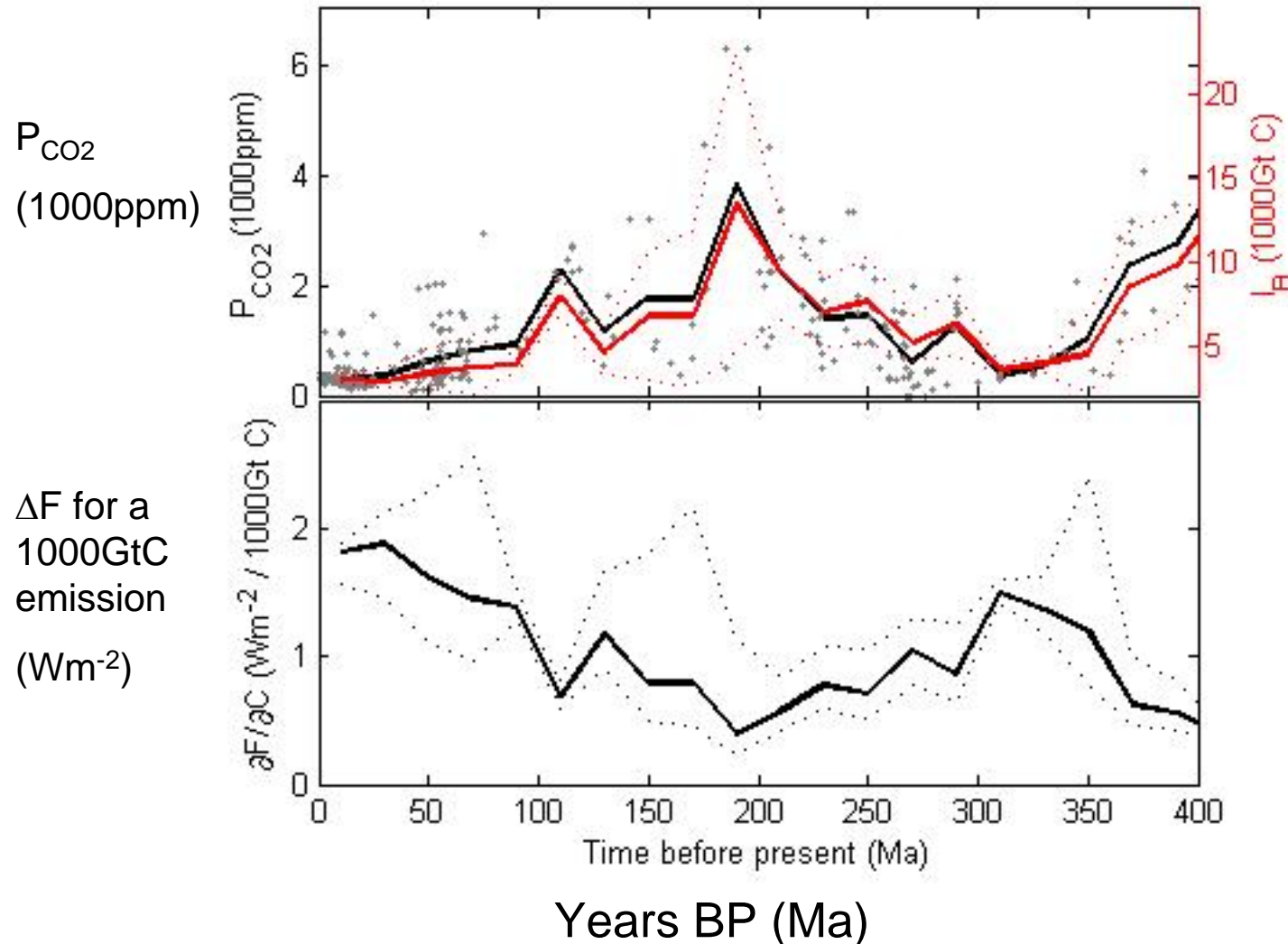
$$\Delta F = \frac{\alpha}{I_B} \Delta I_{em}$$

Using IPCC [2001]  $\alpha$ , we find for MITGCM:

$$\Delta F = 1.7 W m^{-2} \text{ per } 1000 \text{ Gt C}$$

- The contribution of today's emissions to the climate from 1000 to 5000 years
- cf current forcing  $\sim 1.6 W m^{-2}$  in transient state
- Possibly rising to  $\sim 7.5 W m^{-2}$  lasting for thousands of years

## Climate sensitivity of the past



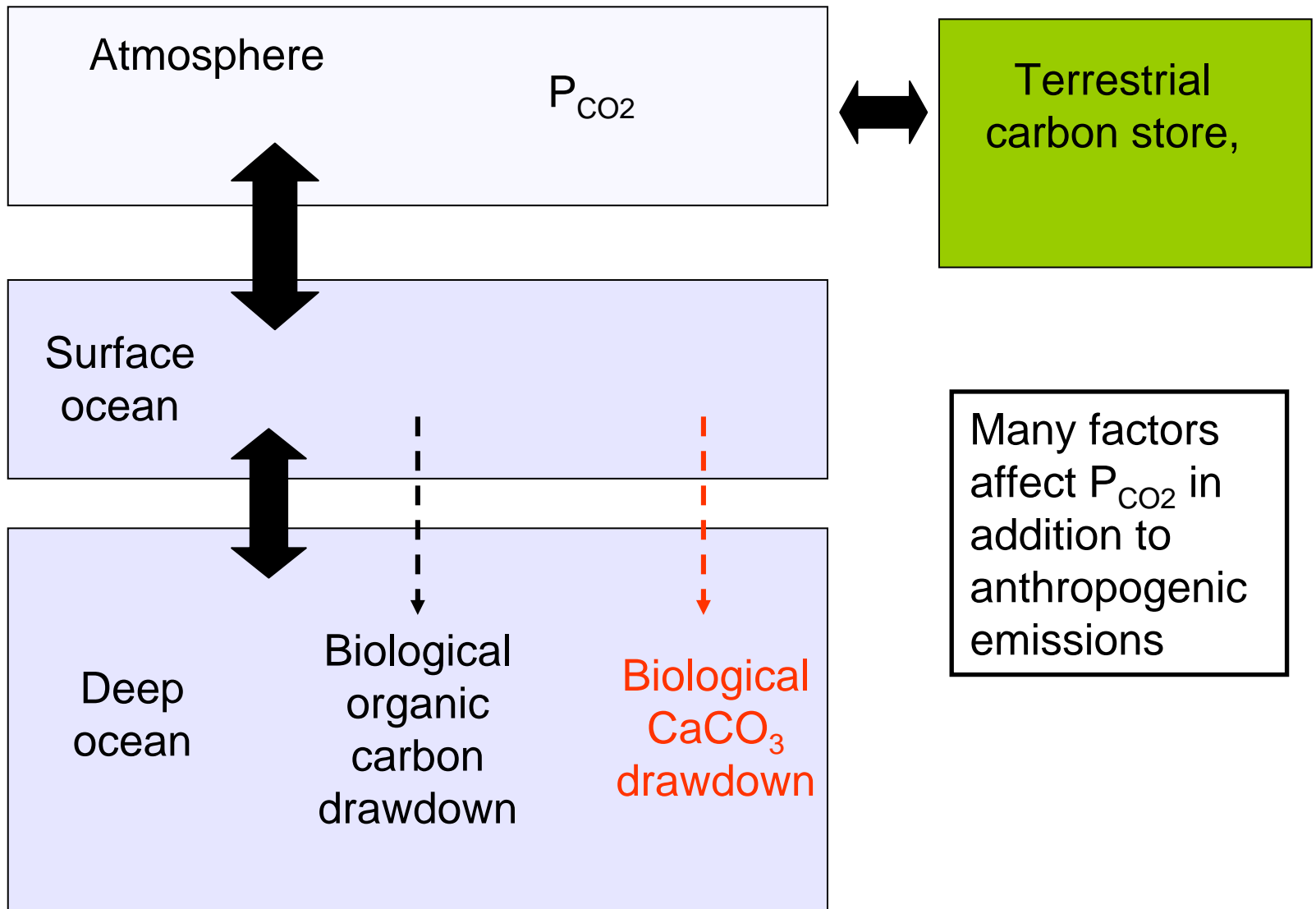
Evaluate  $I_B$  of GENIE model forced with palaeo constraints from Ridgwell (2005)

$$\frac{\delta F}{\delta I_{em}} = \left( \frac{\alpha}{I_B} \right)$$

The present day has a high climate sensitivity

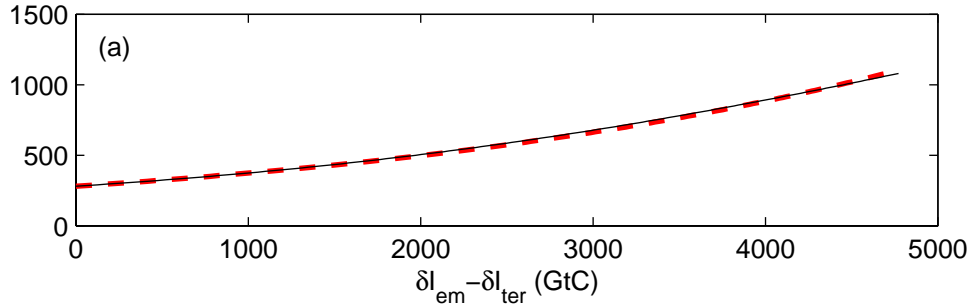
# CONSIDERING CARBON CYCLE FEEDBACKS

## Feedbacks from carbon cycles changes



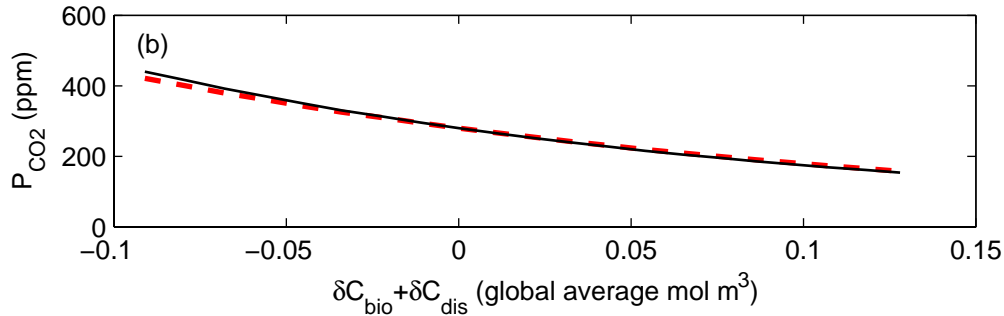
## Testing the independent analytical relations

Evaluate  $I_B$  at pre-industrial steady state and plot:



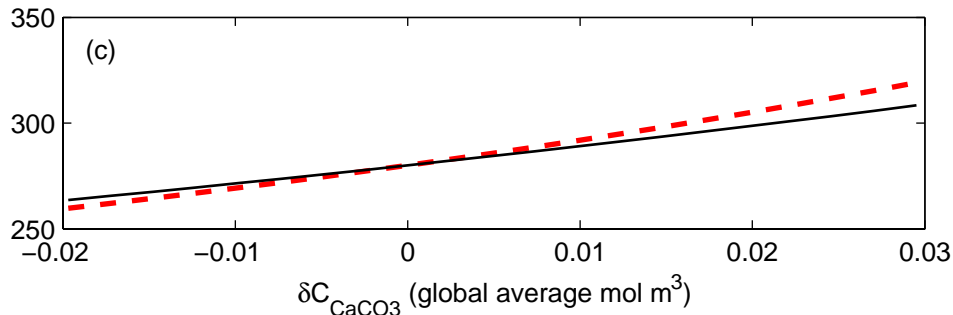
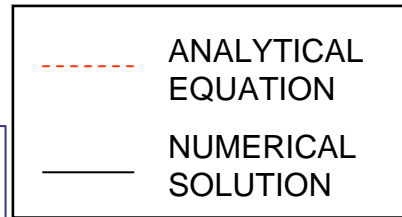
Terrestrial

$$P_f = P_i \exp\left(\frac{-\Delta I_{ter}}{I_B}\right)$$



Soft tissue

$$P_f = P_i \exp\left(\frac{-V\Delta C_{bio}}{I_B}\right)$$



CaCO3

$$P_f = P_i \left[ \frac{I_{O(A-C)}}{I_{O(A-C)} - V\Delta C_{CaCO_3}} \right] \exp\left(\frac{-(I_A/I_{O(A-C)})\Delta C_{CaCO_3}}{I_B}\right)$$

# CONSIDERING CARBON CYCLE FEEDBACKS

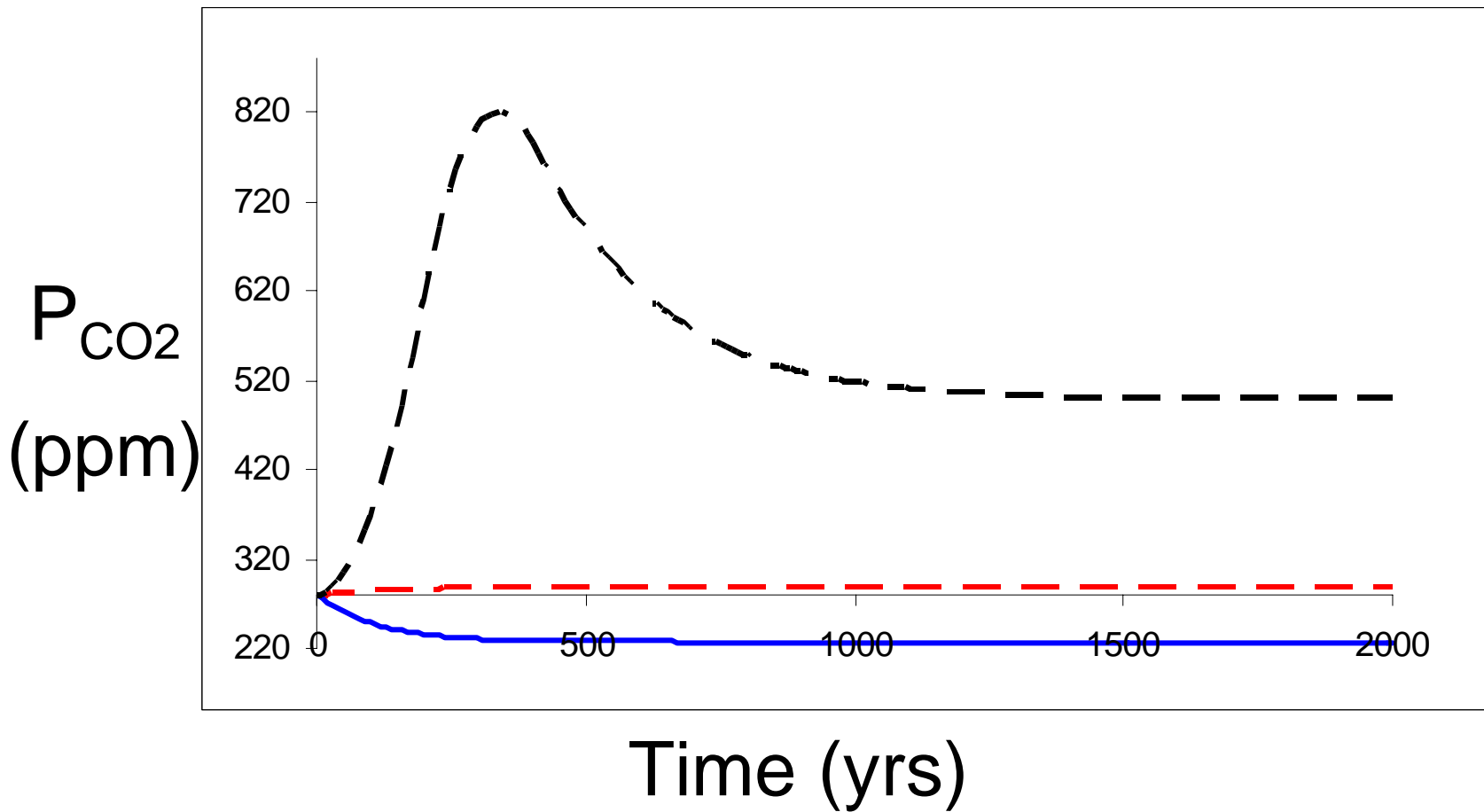
## Feedbacks from carbon cycles changes

$P_{\text{CO}_2}$  over time for:

i) 2000GtC emission,

ii) **Change in soft tissue biology,**

iii) **Change in biological  $\text{CaCO}_3$  production**

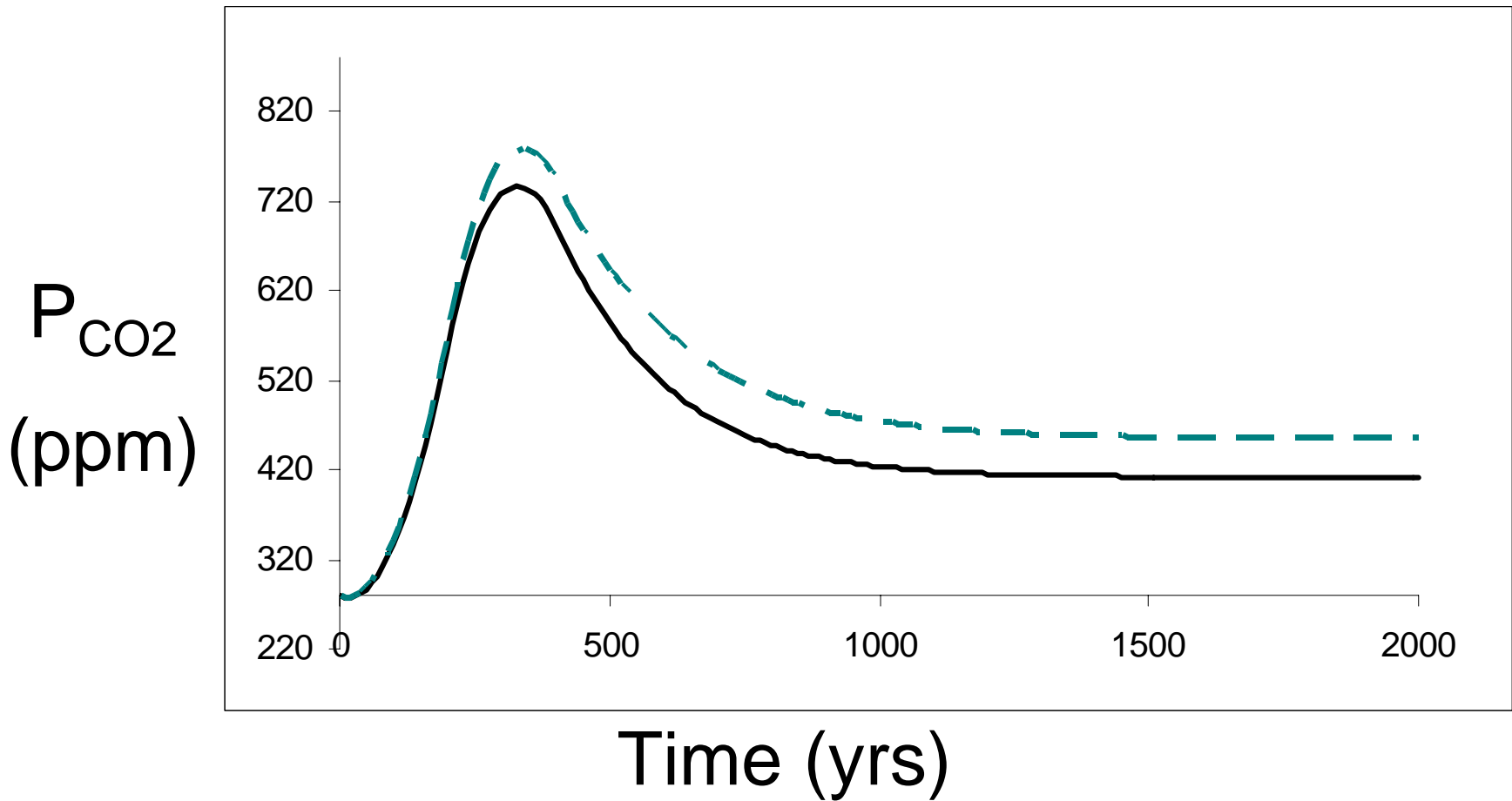


# CONSIDERING CARBON CYCLE FEEDBACKS

## Feedbacks from carbon cycles changes

Feedbacks combine in a non-linear way to alter  $P_{CO_2}$

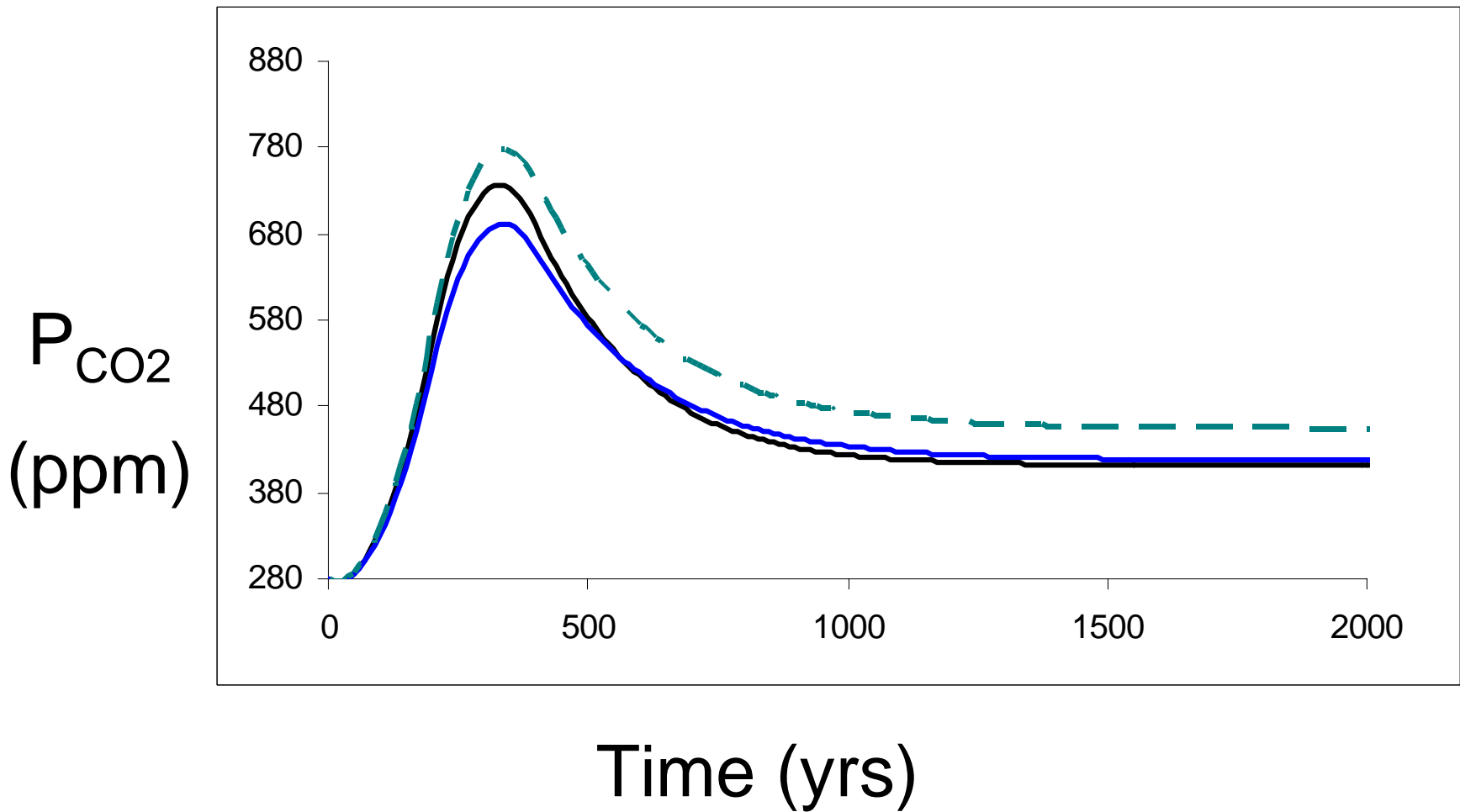
$$(\Delta P_{CO_2})_{overall} \neq (\Delta P_{CO_2})_{EMISSION} + (\Delta P_{CO_2})_{SOFT-TISSUE} + (\Delta P_{CO_2})_{CaCO_3}$$



# CONSIDERING CARBON CYCLE FEEDBACKS

## Feedbacks from carbon cycles changes

Maths predicts: 
$$\left(\frac{P_{CO_2}}{P_0}\right)_{overall} = \left(\frac{P_{CO_2}}{P_0}\right)_{EMISSION} \times \left(\frac{P_{CO_2}}{P_0}\right)_{SOFT-TISSUE} \times \left(\frac{P_{CO_2}}{P_0}\right)_{CaCO_3}$$



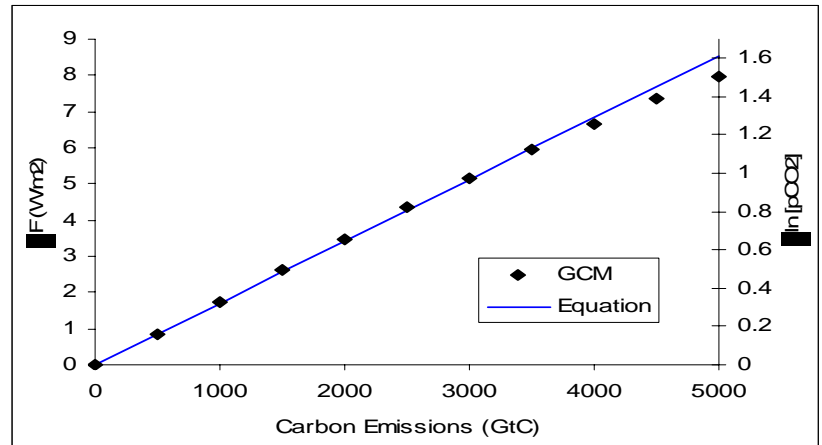
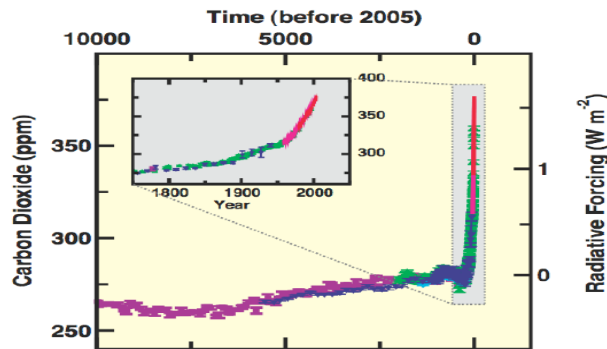


# Conclusions

- Analytical link to numerical models: insight into non-linear feedbacks

$$\left(\frac{P_{CO_2}}{P_0}\right)_{overall} = \left(\frac{P_{CO_2}}{P_0}\right)_{EMISSION} \times \left(\frac{P_{CO_2}}{P_0}\right)_{SOFT-TISSUE} \times \left(\frac{P_{CO_2}}{P_0}\right)_{CaCO_3}$$

- Can compare future steady state forcing to present transient levels:



- Present climate sensitivity to carbon perturbations is large:  $1.7 W m^{-2}$  per 1000 Gt C for thousands of years

# Why should we assume $I_B$ remains constant?

$I_B$  can be expressed in terms of a carbon 'buffer factor',  $B$ :

$$B = \frac{\delta[CO_2]}{[CO_2]} \frac{C_{DIC}}{\delta C_{DIC}}$$

By writing:

$$I_B = I_A + \frac{I_O}{B}$$

While  $B$  increases as  $P_{CO_2}$  increases; they have opposing effects on the value of  $I_B$ . Causing:  $\Delta I_B \ll I_B$

VALID UNTIL ~ 5000GtC

